

# Collisionless Shocks and Particle Acceleration

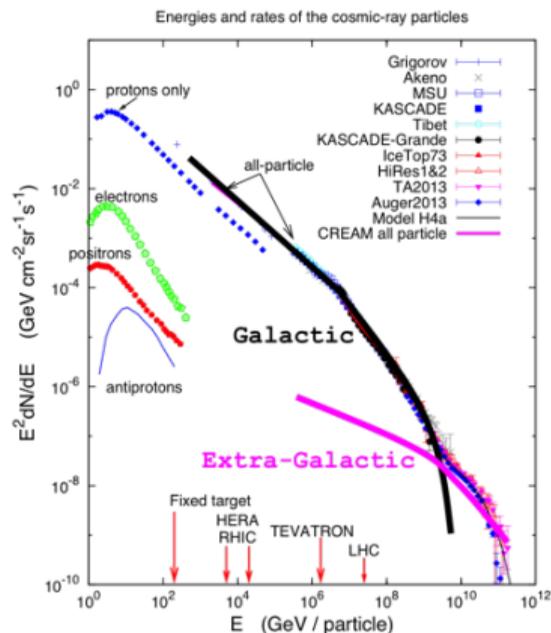
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# Collisionless Shocks and Cosmic Ray Acceleration



IceCube compilation of CR spectrum

- CR energy spectrum was long thought to be a featureless power law:
  - a hallmark of the underlying acceleration mechanism:
    - **diffusive shock acceleration (DSA)** operating in **supernova remnant (SNR) shocks**
- DSA rigidity ( $p/Z$ ) spectra should be the same for all CR species
- Any variations in power-law index are interpreted as changes of acceleration regimes, or sources (galactic-extragalactic, etc.)

# New Era in Observation Technology

- DSA predictions of energy spectra and composition of CRs scrutinized
- **proved not true in many instances**



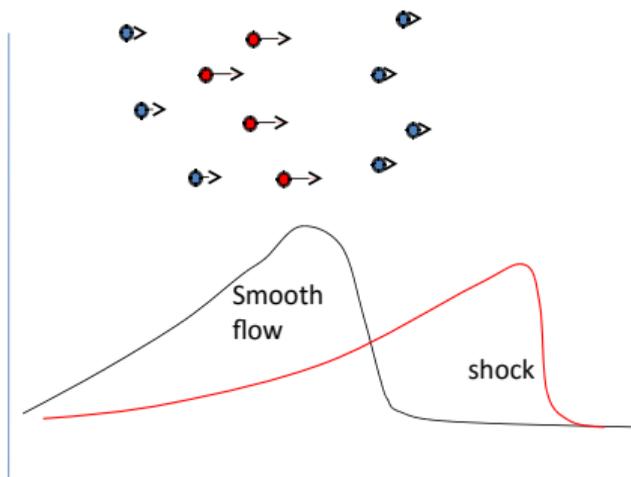
Alpha Magnetic Spectrometer (AMS-02):  
Particle detector operating on the International  
Space Station

- Either we do not quite understand how DSA works or there are additional, (exotic) CR sources, including **dark matter decay or annihilation**
- major problem: lack of understanding of **collisionless shock mechanism**
- especially particle injection into DSA
- elemental selectivity ( $A/Z$  - dependence, not just rigidity?)

# Outline

- 1 Exciting time for the field, challenging time for DSA
  - DSA: collisionless shock process
  - SNRs as main source of galactic CRs (“Standard Model” ?)
- 2 Objection 1
  - Anomalies in Helium/proton fraction rigidity spectrum
  - Possible explanations
- 3 Objection 2
  - Positron Anomaly: Charge-sign dependent CR acceleration
  - Physics of rising and falling branches of positron fraction: NL DSA
  - Physics of the spectral minimum
- 4 Conclusions:
  - He/p anomaly: fully accounted for by  $A/Z$  injection dependence
  - Positron Anomaly: Explained but Room for DM/Pulsars contribution

# CR production mechanism: Diffusive Shock Acceleration (DSA)



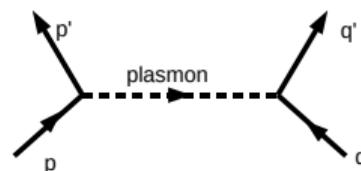
flow velocity

-Most shocks of interest are collisionless

-Big old field in plasma physics

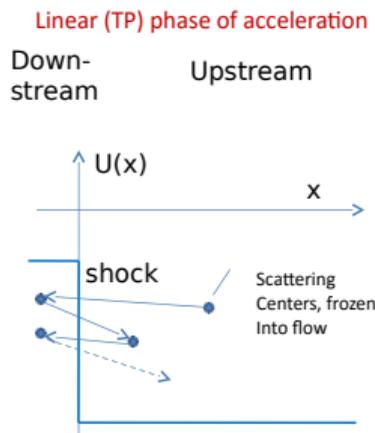
## Problems:

- How to transfer momentum and energy from fast to slow gas envelopes if there are no binary collisions?
- waves. . .
- driven by particles whose distribution is almost certainly unstable. . .

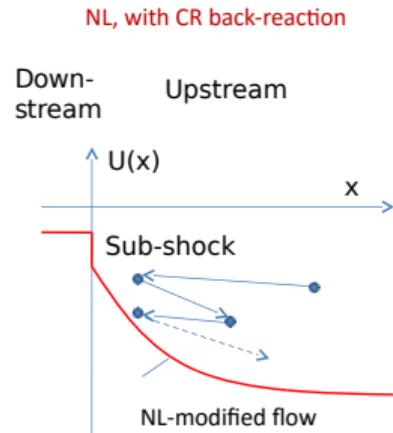


# Essential DSA (aka Fermi-I process, E. Fermi, ~1950s)

DSA giant step: 1977-78: Krymsky, Blandford, Bell, Axford

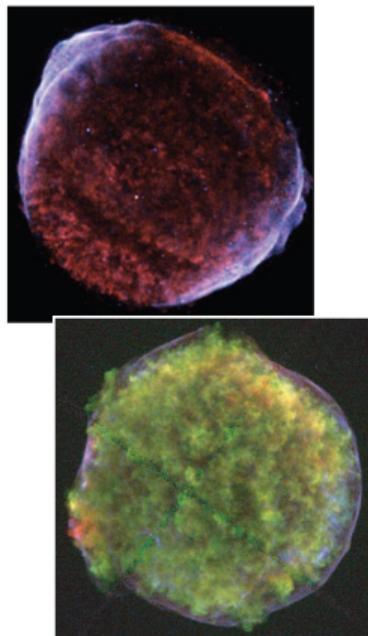


- Particles are trapped between converging mirrors:  $p\Delta x \approx \text{const}$ , MM, P. Diamond, 2006
- $\Rightarrow$  CR spectrum: determined by shock compression,  $r$ :  $f \sim p^{-q}$ ,  $q = 3r/(r-1)$ ,  $r = q = 4$  for strong shocks  $M \rightarrow \infty$



- Index  $q$  becomes  $q(p)$ :
  - soft at low  $p$ :  $q = 3r_s/(r_s - 1)$ ,  $r_s < 4$  ( $\sim 2 - 3$ )
  - hard at high  $p$ :  $q \rightarrow 3.5$  (largely independent of  $r \gg 1$ ) MM, 1997, 1999

# CR acceleration in SNRs



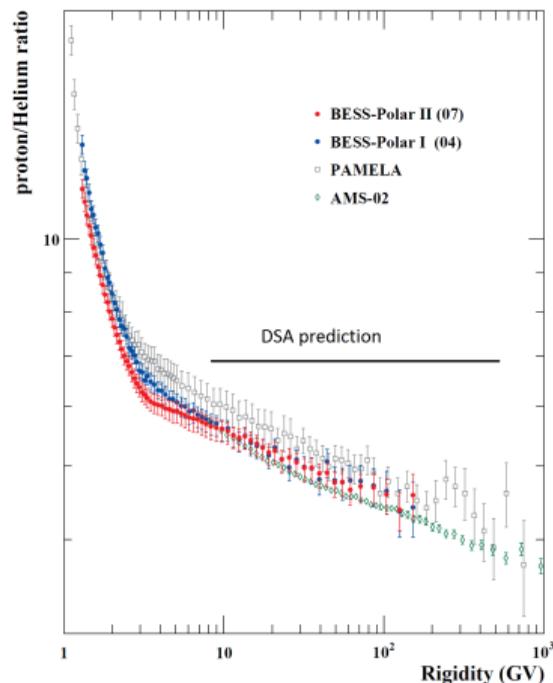
- SN 1006 and SN 1572 (Tycho),  
Reynolds 2008 and Warren et al 2005

- At least some of the galactic SNR are expected to produce CR up to  $10^{15} \text{ eV}$  (knee energy)
- “Direct” detection is possible only as secondary emission
  - observed from radio to gamma
  - electron acceleration up to  $\sim 10^{14} \text{ eV}$  is considered well established, synchrotron emission in x-ray band (Koyama et al 1995, Bamba et al 2003)
  - tentative evidence of proton acceleration from nearby molecular clouds:

$$pp \rightarrow \gamma$$

Fermi-LAT, HESS, Agile,...

# Pamela p/He Anomaly



- The PAMELA orbital telescope revealed deviation ( $\approx 0.1$  in spectral index) between He and protons, deemed inconsistent with DSA (Adriani et al 2011)
- DSA predicts a flat spectrum for the He/p ratio
- similar result obtained recently by AMS-02 for C/p ratio
- points to initial phase of acceleration where elemental similarity (rigidity dependence only) does not apply
- $A/Z$  is the same for He and C

AMS-02 (2015) results along with earlier data

# Suggested explanations of He spectral hardening

- three different types of SNRs contribute [Zatsepin & Sokolskaya \(2006\)](#)
- outward-decreasing He abundance in certain SNR, such as super-bubbles, result in harder He spectra, as generated in stronger shocks [Ohira & Ioka \(2011\)](#)
- He is neutral when processed by weak shocks. It is ionized when the SNR shocks are young and strong, [Drury, 2011](#)
- spallation processes lead to deficiency of He at lower energies as it has longer confinement time in the Galaxy, [Blasi & Amato 2011](#)
- p/He --Forward/reverse SNR shock, [Ptuskin & Zirakashvili, 2012](#)

## Issues:

- most suggestions hard to reconcile with Occam's razor approach
- tension with the He-C striking similarity
- spallation scenario overproduces CR secondaries

# Simple Proof of Elemental Invariance

- write equations using rigidity instead of momentum,  $\vec{\mathcal{R}} = \mathbf{p}c/eZ$

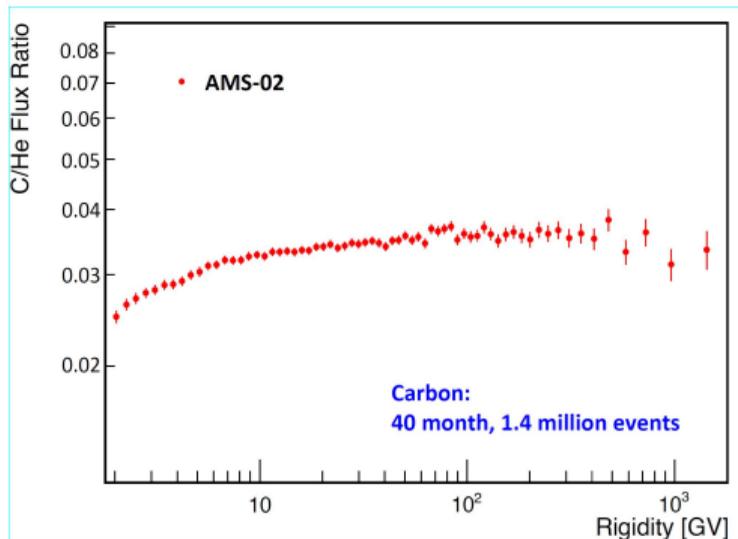
$$\frac{1}{c} \frac{d\vec{\mathcal{R}}}{dt} = \mathbf{E}(\mathbf{r}, t) + \frac{\vec{\mathcal{R}} \times \mathbf{B}(\mathbf{r}, t)}{\sqrt{\mathcal{R}_0^2 + \mathcal{R}^2}}$$

$$\frac{1}{c} \frac{d\mathbf{r}}{dt} = \frac{\vec{\mathcal{R}}}{\sqrt{\mathcal{R}_0^2 + \mathcal{R}^2}}$$

where  $\mathcal{R}_0 = Am_p c^2 / Ze$ ,  $A$  -atomic number

- if  $p$ 's and  $\text{He}^{2+}$  start acceleration at  $\mathcal{R} \gg \mathcal{R}_0$  in a ratio  $N_p/N_{\text{He}}$
- this ratio is maintained in course of acceleration and the rigidity spectra are identical
- if both species propagate to observer without collisions, they maintain the same  $N_p/N_{\text{He}}$
- DSA predicts distribution  $\propto \mathcal{R}^{-q}$  where,  $q$  depends on Mach number as  $q = 4 / (1 - M^{-2})$

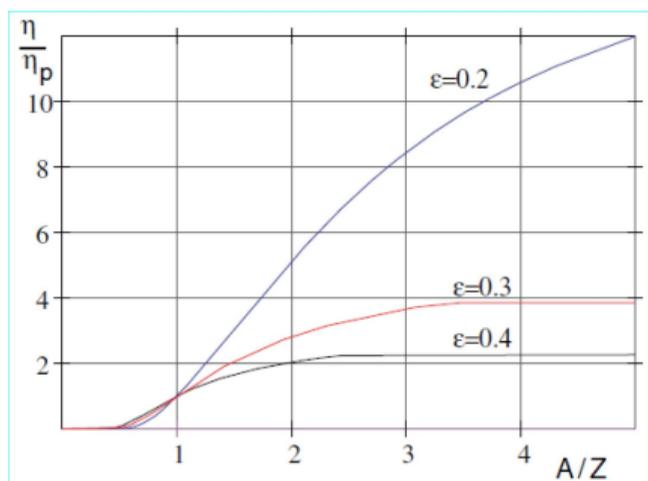
# Recent AMS-02 hint on the origin of p/He Anomaly



- AMS-02 (2015) from M. Heil talk at CERN (not yet official)

- flat C/He ratio eliminates most scenarios
- points to initial phase of acceleration, *injection*, where elemental similarity (rigidity dependence only) does not apply
- $A/Z$  is the same for He and C
- $\mathcal{R}_0 = Am_p c^2 / Ze$  that determines the injection from thermal plasma also the same

# Occam's approach to resolve Pamela puzzle within DSA



Injection efficiency (normalized to proton, MM'98)

## Assumptions:

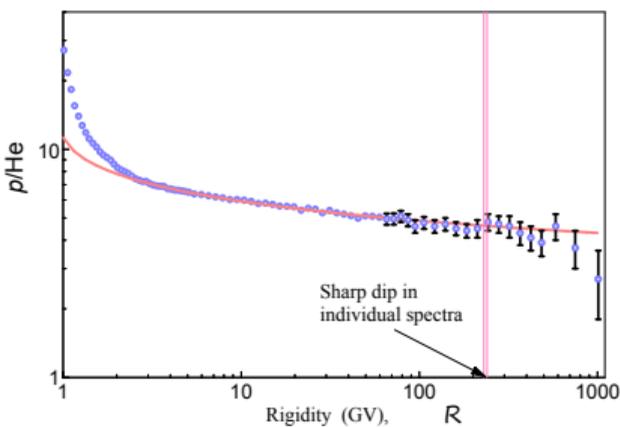
- single source (SNR)
  - shock propagates into ionized homogeneous plasma

- shock radius and Mach number evolve according to Sedov-Taylor point explosion

## Main ideas:

- preferential injection of He into DSA for higher Mach numbers
- injection dependence on  $A/Z$  and on  $\epsilon$ , inverse wave amplitude  $\epsilon \sim B_0/\delta B$
- $\epsilon$  decreases with growing Mach number
- injection bias is due to Alfvén waves driven by protons, thus retaining protons downstream more efficiently than He and C

# p/He ratio integrated over SNR life



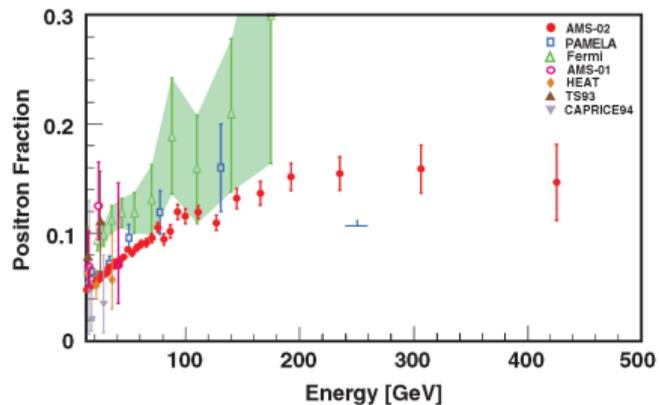
He/p from MM, Diamond and Sagdeev, 2012

- automatically predicts the p/C ratio since the rest rigidity ( $A/Z$ ) is the same for C and He

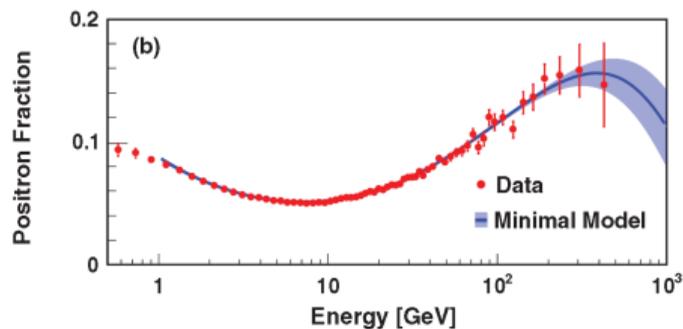
## Some Conclusions

- the p/He ratio at  $\mathcal{R} \gg 1$ , is not affected by CR propagation, regardless the individual spectra
- telltale signs, intrinsic to the particle acceleration mechanism
- reproducible theoretically with no free parameters
- PIC and hybrid simulations will be instrumental in computing p and He injection scalings with Mach number, e.g. [Hanusch et al, APS 2016](#), + [in preparation](#)

# Positron Anomaly (excess)



- Positron excess ([Accardo et al 2014](#))
- Observed by different instruments for several years
- Dramatically improved statistics by AMS-02 (published in 2014)



Things to note:

- Remarkable min at  $\approx 8$  GeV
- Unprecedented accuracy in the range 1-100 GeV
- Saturation (slight decline?) trend beyond 200 GeV
- Eagerly awaiting next data release!

# Suggested explanations of positron excess

- Early explanations focused on the rising branch of positron anomaly
- Most of the SNR related suggestions invoke secondary  $e^+$  produced by galactic CR protons colliding with:
  - ambient dense gas in surroundings of SNR accelerator (Fujita+ 2009)
  - elsewhere in the Galaxy (Blum+2013, Cowsik+ 2014)
  - immediately at shock front (Blasi 2009, Mertsch 2014, Cholis+ 2014)
- Tensions with  $\bar{p}$  observations (should show similar trends, as both are secondaries)
- Poor fits to high-precision AMS-02 data or too many *ad hoc* assumptions (e.g. **multiple sources** with, often, arbitrary power-law indices)
- Tensions with  $\gamma$ -s

## Further explanations

- **Pulsars** (e.g. Profumo 2012, big review). Possible, but have disadvantage of lacking accurate acceleration models
- **Dark matter** contribution ??
- Positrons injected into DSA by radioactive elements of SN ejecta

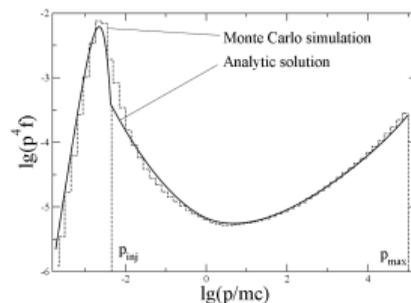
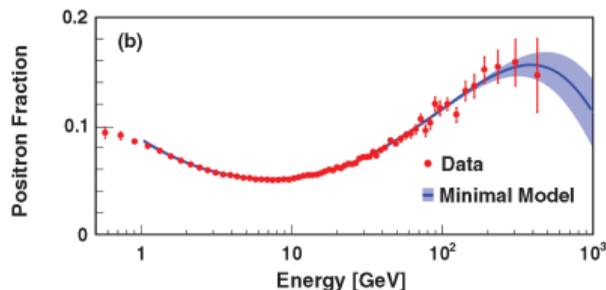
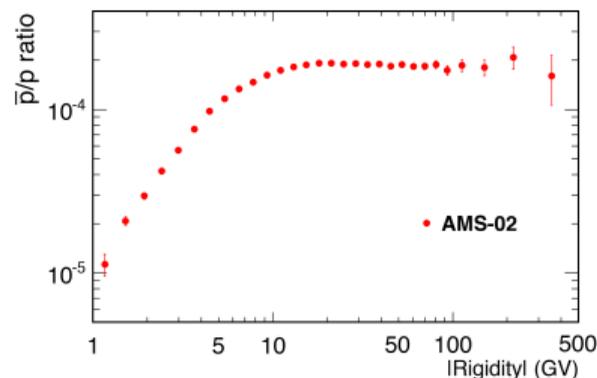
### Obvious remarks

- Pulsars and particularly DM have much weaker predictive capabilities than the DSA-SNR- based models
- should be considered if the SNR contribution falls short to account for positron excess
- SNR contribution to the phenomenon constrains possible DM/pulsar contributions

## Desirable aspects of the mechanism (Wishlist)

- account for  $e^+$  fraction by a single-source, a nearby SNR
- explain physics of decreasing and increasing branches
- identify physics of the minimum at 8 GeV
- understand  $\bar{p}$  flat spectrum as intrinsic, not coincidental: most likely, accelerated just like protons, whenever injected BUT:  $\bar{p}/p \neq e^+/e^-$
- $\implies$  acceleration mechanism ought to be *charge-sign dependent*
- physics of charge-sign selectivity

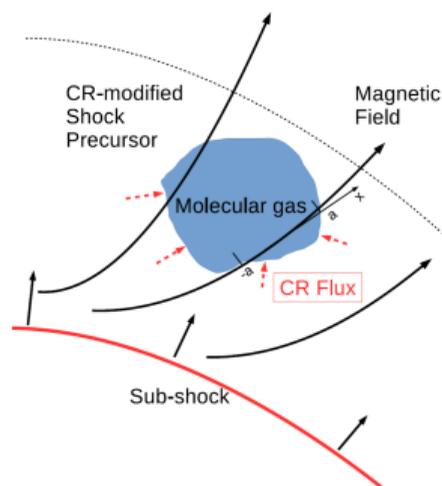
# The Hints



(AMS Days at CERN, Kounine 2015)

- $\bar{p}$  fraction is flat on the rising  $e^+$  fraction branch  $E > 8$  GeV
- Opposite trends on the declining  $e^+$  fraction branch  $E < 8$  GeV
- Both data sets relate to fractions, thus eliminating all charge-sign independent aspects of propagation and acceleration
- Striking similarity with NL DSA solution (MM, 1997), assuming most of  $e^-$  are accelerated to  $p^{-4}$  (standard DSA)

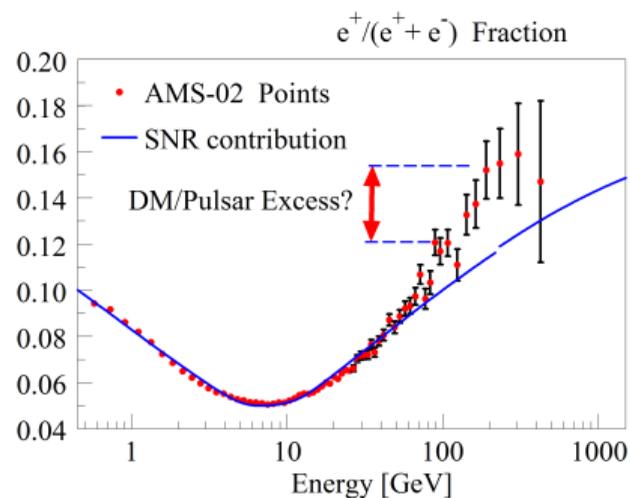
# Assumptions of the present model



- shock propagates in “clumpy” molecular gas,  $n_{\text{H}} \gtrsim 30 \text{cm}^{-3}$   $f_{\text{V}} \sim 0.01$ , big mass
- SNR is nearby, likely magnetically connected, big contribution to local CRs

- Other SNRs of this kind may or may not contribute
- Moderately oblique shock
- High-energy protons are already accelerated to  $E \gtrsim 10^{12} \text{eV}$  to make a strong impact on the shock structure (CR back reaction, NL shock modification)
- Acceleration process transitioned into efficient regime (hard to avoid for  $E \gtrsim 1 \text{TeV}$ ,  $M \gtrsim 10 - 15$  and the fraction of accelerated  $p$ 's  $\sim 10^{-4} - 10^{-3}$ )

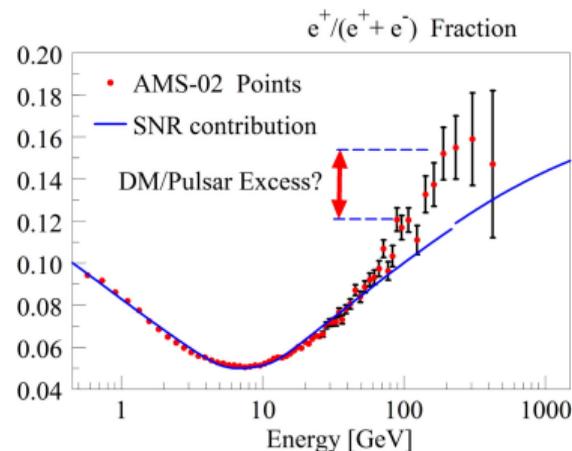
# Salient Features of Calculated Positron Spectrum (MM, Diamond, Sagdeev 2016)



- Shock structure is created by accelerated protons through their pressure distribution

- $e^+$  and other secondaries produced in  $pp$  collisions of shock accelerated CRs with MC gas, as well as  $e^-$  are treated as test particles in this shock structure
- positively charged particles are enhanced while negatively charged suppressed because of charge-asymmetric injection from MC
- $e^+/e^-$  injection rate  $\gg 1$ .

# $e^+$ Spectrum Cont'd



- In calculating  $e^+/(e^- + e^+)$ ,  $e^-$  are assumed to be from conventional shocks with  $p^{-4}$  source spectra
- $\implies e^+/(e^- + e^+)$  spectrum = proton spectrum in  $p^4 f(p)$  customary normalization

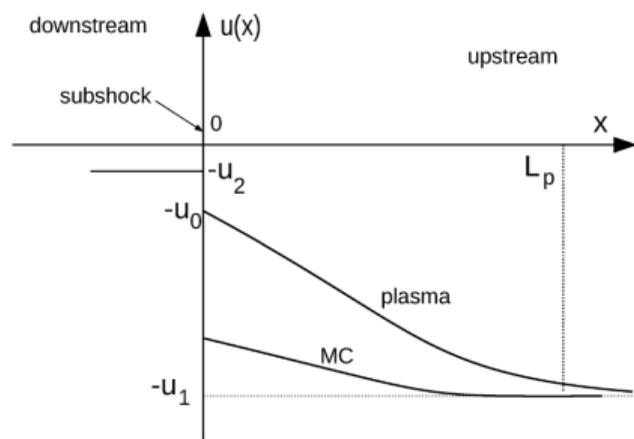
- background  $e^-$  (with  $p^{-4}$  spectrum) propagate distance similar to that of  $e^+$
- $\implies$  ratio  $e^+/(e^- + e^+)$  is de-propagated and probes directly into the **positron accelerator!**
- excess above the blue curve is not SNR – e.g., **DM or pulsars**
- as SNR contrib. is rising with  $E$ , constraints on DM signal in 200-400 GeV range are weaker compared to secondary  $e^+$ (decaying) without acceleration

# Conclusions

- ① A weakly ionized dense molecular cloud (MC) in SNR shock environment, illuminated by shock accelerated protons results in the following phenomena:
  - ① penetrating protons charge MC positively
  - ② secondary positrons produced in  $pp$  collisions inside the MC are pre-accelerated by the MC electric field and injected into DSA
  - ③ most of the negatively charged light secondaries ( $e^-$ ), and to some extent,  $\bar{p}$ , remain locked inside the MC
- ② the spectrum of accelerated  $e^+$  has the observed concave form due to steepening caused by NL subshock reduction, and flattening resulting from acceleration in the smooth part of the shock transition
- ③ the crossover pinpoints the 8 GeV minimum in the  $e^+/(e^+ + e^-)$  fraction measured by AMS-02
- ④ The AMS-02 positron excess in the range  $\sim 200 - 400\text{GeV}$  is not accounted for by the SNR positron spectrum and is available for alternative interpretations (DM, Pulsars, ???)

# Back up slides

# Electrodynamics of CR-MC interaction



- MC move faster (in the shock frame) than the upstream flow (bow-shocks form)
- CR number density in MC increases explosively:

$$n_{CR}(t) = n_{CR}^0 x_0 / (x_0 - u_1 t)$$

- Reaction from the MC:
- buildup of electric field of a *positive* electrostatic potential
- minus-charge particles are attracted and stay inside MC during the subsequent shock crossing  $\rightarrow$  evade acceleration
- plus-charge particles are expelled and injected into DSA
- charge-sign asymmetry of injection/acceleration

## Short digression into elementary plasma physics

- plasmas enforce almost “zero-tolerance” policy in regard to violation of their charge neutrality

### Example

take  $1\text{cm}^3$  of air

ionize and separate  $p$  and  $e$  to distance  $r = 0.5\text{ cm}$

the resulting force

$$F = e^2 N^2 / r^2 \sim 10^{16} \text{ lb}$$

As  $N \sim 10^{19}$ ,  $I = 13.6\text{ eV}$

ionization energy only  $\sim 100\text{ Joules}$

- similarly, injection of an external charge into plasma must lead to enormous electrostatic forces
- key words here are “separate” and “inject”
- need a powerful mechanism
- energetic CBs can do that

- Two-fluid equations:

$$\begin{aligned}\frac{dV_i}{dt} &= \frac{e}{m_i} E(x, t) - \nu_{in} V_i \\ \frac{dV_e}{dt} &= -\frac{e}{m_e} E - \nu_{ei} (V_e - V_i) \\ \frac{\partial n_{e,i}}{\partial t} &= -\frac{\partial}{\partial x} n_{e,i} V_{e,i} \\ n_e &= n_i + n_{CR}\end{aligned}$$

- Electric field is related to CR charging rate and ion outflow:

$$E(x, t) = \frac{m_e}{e} \nu_{ei} \frac{n_{CR}}{n_{CR} + n_i} \left( \frac{\dot{n}_{CR}}{n_{CR}} x + V_i \right)$$

## Self-similar solution

- Ions leave the MC symmetrically:  $V_i(x, t) = xV(t)$ ,  $E \propto V_i$ , assuming  $x = 0$  being a midpoint of the field line threading the MC,  $|x| \leq a$
- All other solutions converge to this form
- Electric field ( $-\infty < t < 0$ ):

$$E(x, t) \simeq \frac{m_i}{e} a v_{in}^2 \frac{x\alpha}{(t_0 - t)^2} \left[ 1 + \frac{\alpha}{t_0 - t} \right]$$

with dimensionless parameter that characterizes ion depletion

$$\frac{\alpha}{t_0} \sim \left( \frac{1\text{eV}}{T_e} \right)^2 \frac{n_{CR}^0}{n_n} \sqrt{\frac{m_n}{m_i} \left( \frac{m_n}{m_i} + 1 \right) \frac{m_e}{m_i}} \sim \Delta n_i / n_i \ll 1$$

( $t$  measured in  $i - e$  collision times)

## Solution for electric field in MC, cont'd

- Maximum electric field (at MC edge)

$$E_{\max} \simeq \frac{m_e}{e} u_1 \nu_{ei} \frac{n_{CR}^0}{n_i}$$

- electrostatic potential with a maximum in the middle of the MC ( $x = 0$ ) screens the MC interior from penetrating CR

$$\frac{e\phi_{\max}}{m_p c^2} \sim \frac{a}{1pc} \frac{u_1}{c} \frac{n_{CR}}{1cm^{-3}} \left( \frac{1eV}{T_e} \right)^{3/2}$$

- A 1-parsec MC ( $r_g$  of a PeV proton) is acceptable as it occupies only a  $u_1/c \ll 1$ - fraction of CR precursor
- electric field is strong enough to keep low-energy CRs away from the MC interior
- keeps secondary  $e^-$  (and  $\bar{p}$ , to much lesser extent) inside, ejects secondary  $e^+$
- charge sign asymmetry of injection into DSA established

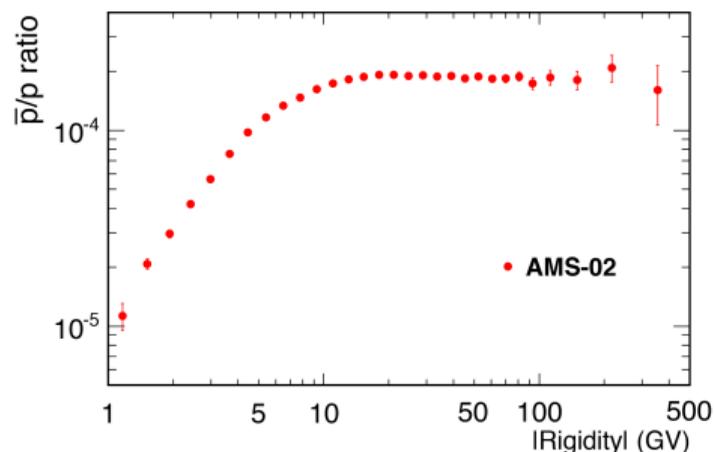
# Positron Injection into DSA

- secondary  $e^+$  are largely produced deep inside MC, preaccelerated in  $E$  and easily injected into DSA
- injection from many MCs occasionally crossing the shock occurs with a time-averaged rate  $Q(p, x)$
- $Q$  decays sharply with  $x$ , the distance from the subshock
- it has a broad maximum at  $p \sim e\phi_{\max}/c$
- near subshock, CR number density sharply increases on account of GeV particles. They generate secondary  $e^\pm$  and  $\bar{p}$ , on the periphery of MC. The edge electric field then expels positively charged secondaries ( $e^+$ ) and sucks in negatively charged ones, such as  $e^-$  and, to some extent,  $\bar{p}$
- typical energy of expelled positrons  $< 1 - 2$  GeV

# Shock Acceleration of Positrons

- As the shock is modified, acceleration starts in its precursor since  $\partial u / \partial x \neq 0$
- However, most of the positrons are released from the MC near the subshock
- at lower energies, their spectrum is dominated by the subshock compression ratio,  $r_s = u_0 / u_2$
- spectral index  $q = q_s \equiv 3r_s / (r_s - 1)$  and the spectrum  $f_{e^+} \propto p^{-q_s}$ .
- at higher energies, positrons feel progressively higher flow compression (diffuse farther ahead of the subshock)
- their spectrum tends to a universal form with  $q \rightarrow 3.5$

# Antiprotons



- If most of  $\bar{p}$  and  $p$  come from the same source as  $e^+$  ( $\bar{p}$  generated in MCs ahead of SNR shock), the  $\bar{p}$  spectrum should be the same as  $p$  at  $E \gtrsim 10$  GeV

- Similarly,  $\bar{p}/p$  should be flat if  $\bar{p}$  are injected as secondaries into any SNR-DSA process
- Decline of  $\bar{p}$  towards lower energies is consistent with electrostatic retention in MC
- This effect has not been quantified for  $\bar{p}$
- Solar modulation may also contribute to  $p - \bar{p}$  difference at low energy
- Flat  $\bar{p}/p$  should continue till  $p_{\max}$  then it should start declining (secondaries with no acceleration)