Co-current toroidal rotation driven and turbulent stresses with resonant magnetic perturbations in the edge plasmas of the J-TEXT tokamak


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Abstract: The acceleration of the co-current toroidal rotations around resonant surfaces by resonant magnetic perturbations (RMPs) through turbulence is presented. These experiments were performed using a Langmuir probe array in the edge plasmas of the J-TEXT tokamak. This study aims at understanding the RMP effects on edge toroidal rotations and exploring its control method. With RMPs, the flat electron temperature $T_e$ profile due to magnetic islands appears around resonant surfaces [K. J. Zhao et al., Nucl Fusion, 55, 073022 (2015)]. When the resonant surface is closer to the last closed flux surface, the flat $T_e$ profile vanishes with RMPs. In both cases, the toroidal rotations significantly increase in the direction of the plasma current around resonant surfaces with RMPs. The characteristics of turbulence are significantly affected by RMPs around resonant surfaces. Turbulence intensity profile changes and the poloidal wave vector $k_\theta$ increases with RMPs. The power fraction of the turbulence components in the ion diamagnetic drift direction increases with RMPs.
The measurements of turbulent Reynolds stresses are consistent with that the toroidal flows can be driven by turbulence. The estimations of the energy transfer between turbulence and toroidal flows suggest that turbulence energy transfers into toroidal flows. The result has the implication of the intrinsic rotation being driven by RMPs via turbulence.

1. Introduction

Interaction of magnetohydrodynamic (MHD) structures and flows is a subject of general interest in physics. Typical examples include magnetic braking of stellar rotation [1], angular momentum transport in astrophysical disks [2, 3], and dynamics of the earth core and geodynamo [4]. In fusion plasmas, the study of interactions between plasma flows and resonant magnetic perturbations (RMPs) aims at understanding and controlling plasma confinement and transport. RMPs have significant effects on the profiles and cross field transport [5–14], and are applied to mitigate the large scale edge local mode (ELM) in tokamak plasmas [15].

The toroidal rotation has been widely recognized to play an important role in plasma confinement improvement [16–17] and MHD stabilization [18–19] in tokamaks and in helical devices. There are various driving mechanisms for toroidal rotations and some of them have already been well documented. They are: external momentum input, such as neutral beam injection; spontaneous/intrinsic rotation without apparently momentum input [20–25]. The intrinsic rotation can be caused by residual Reynolds stresses due to turbulence. The residual stress is a part of the total Reynolds stress. It is independence of the velocity and velocity gradient, and only depends on the characteristics of turbulence, the temperature gradient, density gradient and pressure gradient etc. A new turbulent acceleration term which has different physics from the residual stress was found to drive the co-current rotation using gyrokinetic theory [26]

RMPs can generate not only stochastic magnetic fields, but also coherent magnetic islands. RMP-induced stochastic regions and magnetic islands have strong effects on turbulence [9–14, 27]. The common feature is that the radial electric field $E_r$ increases
in stochastic and magnetic island regions [11-13, 27-29]. The phase delay between the plasma edge density and electron temperature depends on the relative rotation of the RMP field and the toroidal plasma rotation [30]. The plasma flow is also influenced by RMPs [11, 31]. The RMP braking effects on the toroidal rotation were observed in the core plasmas in most devices [32]. The opposite effects - the acceleration of toroidal rotations due to RMPs - were detected in a few devices. With small injected neutral beam momentum, the toroidal rotation is accelerated in a direction counter to the plasma current due to RMPs [33]. The deeply penetrating RMPs of m/n=3/1 mode configuration increases the toroidal plasma rotation and the toroidal rotation is always in the direction of the plasma current [34]. In the edge tokamak plasmas, the acceleration of the toroidal rotation due to RMPs was also measured [27-29]. However, the correlation between the acceleration of toroidal rotations and turbulence with RMPs has not been studied although this is a crucial issue because of its relevance to intrinsic rotation.

Here, the acceleration of the toroidal rotation in the direction of the plasma current around resonant surface in the edge tokamak plasmas with RMPs is presented. The characteristics of turbulence around resonant surface are varied when the RMP coils are applied. With RMPs, the turbulence energy around resonant surface transfers into toroidal flows. This observation suggests that the acceleration of the toroidal flow is relevant to the change of the turbulent characteristics around resonant surface with RMPs.

The rest of this work is organized as follows. The experimental set-up is given in section 2. The experimental results, described in section 3, include the acceleration of the toroidal rotation with RMPs, the radial dependences of the plasma parameters with RMPs, RMP effects on turbulence characteristics and turbulent Reynolds stress, etc. Section 4 presents the conclusion and discussion.
2. Experiment setup

The experiments presented here were conducted in Ohmic plasmas with circular cross section on the J-TEXT tokamak. The major and minor radii of the J-TEXT tokamak are R = 1.05 m and a = 0.255 m, respectively [35]. The plasma parameters for the experiments are the toroidal magnetic field \( B_t = 1.5-2.0 \) T, the plasma current \( I_p = 150-180 \) kA, the line averaged electron density \( N_e = 1-3 \times 10^{19} m^{-3} \), and the edge safety factor \( q_a = 3.1-4.3 \). A set of coils, called a dynamic RMP, has been installed inside the vessel on J-TEXT to study the interaction between helical perturbations and magnetized plasmas, and explore a possible method for control of tearing modes [36]. In the present study, the static configuration of RMP was used. The base mode and strength of the magnetic perturbation were varied by adjusting the power supply to the coils. The perturbation field strength of \( B_r \sim 5.42 \times 10^{-5} \) T for \( m/n = 3/1 \) mode, and of \( \sim 1.16 \times 10^{-5} \) T for \( m/n = 4/1 \) mode can be obtained for 1kA in the coils assuming no plasma response. Here, \( m \) and \( n \) are the poloidal and toroidal mode numbers, respectively. The maximum RMP current is 6.5 kA. A fast reciprocating probe array with two steps and 12 tips as shown in figure 1 yields the profiles of floating potential, temperature, density, Mach number, etc. It was mounted on the top of the tokamak. The length and diameter of the tips are 3 mm and 2 mm, respectively. The digitizer can handle fluctuation data up to 2 MHz.

3. Experimental results

3.1 Increase of edge toroidal rotation velocity near resonant surface with RMPs

The increase of the edge toroidal rotation velocity is detected with resonant magnetic perturbations in the edge plasmas of the J-TEXT tokamak. Figure 2 provides the radial profiles of the edge toroidal rotation velocity with RMP current scan. The positive (negative) sign of the toroidal rotation velocity means in the co-current (counter-current) direction. The edge safety factor and the line averaged electron density are \( q_a = 3.1 \) and \( N_e = 2.2 \times 10^{19} m^{-3} \), respectively. The toroidal rotation is measured with a Mach probe array. The Mach number can be estimated as
$M_{mach}=0.4\ln(I_{s-up}/I_{s-down})$, where $I_{s-up}$ and $I_{s-down}$ are the sheath currents collected on two Mach probe tips at the up- and down-stream sides, respectively. The toroidal velocity can be calculated as $V_\phi \approx M_{mach}C_s$. The $C_s$ is ion sound speed as $\sim \sqrt{2T_e/m_i}$, here $T_e$ and $m_i$ are the electron temperature and the ion mass, respectively. Inside the LCFS, the toroidal rotation velocity slightly increases first in the co-current direction as the RMP current increases. When the RMP current is above a threshold value $\sim 5\text{kA}$, the toroidal velocity around the $q=3$ resonant surface in the interval $-1.0 < \Delta r < -0.2\text{cm}$ rapidly increases in the co-current direction, by up to $10\text{km/s}$. Here, $\Delta r$ means the distance from the measurement position to the LCFS and minus means inside the LCFS. In the scrape-off layer (SOL), the toroidal rotation near $\Delta r = 0.8\text{cm}$ also increases first in the co-current direction for increasing RMP current, but when the RMP current is $\sim 6\text{kA}$, the toroidal velocity starts to drop. Compared with the cases inside the LCFS and in the SOL region, the effects of RMPs on the toroidal rotation at the LCFS of $\Delta r \sim 0.0\text{cm}$ are much different. With RMPs, the toroidal rotation changes little at the LCFS. The evolutions of the toroidal rotations in the SOL region might come from the mixing effects of the secondary limiter at $\Delta r$.

![Figure 2](color online) The radial profiles of toroidal rotation velocity with RMP current scan. [The vertical dashed-dot line indicated the $q=3$ resonant surface, $B_t\sim 1.6\text{T}$, $I_p\sim 165\text{kA}$, $q_a=3.1$, $N_e\sim 2.2\times 10^{19}\text{m}^{-3}$].

![Figure 3](color online) The radial profiles of toroidal rotation velocity with RMP current scan. [The vertical dashed-dot line indicated the $q=3$ resonant surface, $B_t\sim 1.6\text{T}$, $I_p\sim 160\text{kA}$, $q_a=3.2$, $N_e\sim 3.0\times 10^{19}\text{m}^{-3}$].
due to the RMP assembly and the RMPs. We will not discuss it more. In this paper, the RMP effects on the toroidal rotation around resonant surface will be focused on.

The RMP effects on the edge toroidal rotations in the resonant layers were examined further with edge safety factor qₐ=3.2 and the line averaged density Nₑ~3.0x10^{19}m⁻³. Figure 3 shows the radial profiles of the toroidal rotation velocity with RMP current scan. The evolutions of the toroidal rotation around the resonant surface with RMP current are similar to the cases with qₐ = 3.1, i.e., when RMP current is above ~5kA, the toroidal rotation rapidly increases in the q=3 resonant layer.

3.2 Radial dependences of plasma parameters with 3/1 RMPs

The radial dependences of plasma parameters with and without 3/1 RMPs at qₐ=3.2 are studied. Figures 4 (a)-(d) show the radial profiles of the toroidal rotation velocities, the electron temperatures, the electron densities, and the radial electric fields (Eᵣ), respectively. The RMP current is 6kA and produces a relative magnetic perturbation Bᵤ/B₀ ~ 2 X 10⁻⁴ for the m/n = 3/1 mode without considering the plasma response. With RMPs, the toroidal velocity significantly increases in the direction of the plasma current in the q=3 resonant layer. The shapes of the radial profiles of the electron temperature are significantly different with and without RMPs. Without RMPs, the electron
temperature increases inward, while with RMPs, the electron temperature drops and becomes flattened around the $q=3$ resonant surface. The $T_e$ flat is identified as a direct effect of RMP-induced islands in the previous observation, i.e., with magnetic islands, $T_e$ is flattened inside the islands, while $T_e$ becomes steeper at the island boundaries [11]. The island width is estimated as $\sim 1.0\text{cm}$ from the temperature profiles. In this discharge, the electron density does not drop near the $q=3$ resonant surface with RMPs, as shown in figure 4 (c). The radial electric field changes from negative to positive inside the magnetic islands. This result suggests that the increase of the toroidal rotation velocity is due to the effects of RMP-induced islands.

### 3.3 Radial dependences of plasma parameters with 4/1 RMPs

The radial dependences of the plasma parameters with and without 4/1 RMPs at $q_a=4.3$ are also studied. The radial profiles of the toroidal rotation velocities at $q_a=4.3$ with and without RMPs are given in figure 5(a). The RMP current is $\sim 5\text{kA}$ and produces a relative magnetic perturbation $B_r/B_0 \sim 3 \times 10^{-5}$ for the $m/n = 4/1$ mode without considering the plasma response. The line averaged density is $\sim 2.2 \times 10^{19} \text{m}^{-3}$. Without RMPs, the toroidal rotation is in the counter-current direction around the $q=4$ resonant surface in the interval $-2.5 < \Delta r < -0.7\text{cm}$. With RMPs, the toroidal velocity sharply increases around the $q=4$ resonant surface in the co-current direction. This is similar to the case with 3/1 RMPs. Moreover, the toroidal rotation in the interval $-2.5 < \Delta r < -0.7\text{cm}$ changes its sign from the counter-current direction to the co-current direction. The

![Figure 5](color online) Radial dependences of plasma parameters with and without RMPs at $q_a=4.3$, (a) toroidal rotation velocity, (b) electron temperature, (c) electron density and (d) radial electric field [$N_e \sim 2.2 \times 10^{19} \text{m}^{-3}$, $I_p\sim 150\text{kA}$, $B_T \sim 2.0 \text{T}$].
reversal of the toroidal rotation is not observed with 3/1 RMPs. Similarly, the electron temperature is flattening inside the island and becomes steeper at its boundaries, as shown in figure 5 (b). However, $T_e$ in the island region does not drop. This differs from the cases with 3/1 RMPs, where $T_e$ significantly drops inside the island. Figure 5 (c) presents the radial profiles of the electron density with and without RMPs. Compared with the cases with 3/1 RMPs, the density significantly drops inside the islands. There is no significant difference for the $E_r$ profiles in the 3/1 and 4/1 island regions. With 4/1 islands, the $E_r$ also increases around the $q=4$ resonant surface, as given in figure 5 (d).

![Figure 6](color online) Radial dependences of plasma parameters with and without RMPs at $q_a=4.3$, (a) toroidal rotation velocity, (b) electron temperature, (c) electron density, (d) radial electric field [$N_e \sim 2.2 \times 10^{19}$ m$^{-3}$, $I_p \sim 150$ kA, $B_T \sim 1.9$T].

The radial dependences of the plasma parameters with and without 4/1 RMPs at $q_a=4.1$ are investigated to understand the effects of resonant layer positions on the toroidal rotations. Figures 6(a)-(d) provide the profiles of the toroidal rotation velocities, the electron temperatures, the electron densities, and the radial electric fields ($E_r$), respectively. The RMP current keeps at $\sim 5$kA and the density is $\sim 2.2\times10^{19}$m$^{-3}$. With RMPs, the toroidal rotation also increases in the co-current direction near the $q=4$ resonant surface and are similar to the case with $q_a=4.3$. Compared with the cases with $q_a=4.3$ and 3.2, the $T_e$ flat vanishes near $q=4$ resonant
surface although the $T_e$ drops there. The steeper $T_e$ profile also forms in the interval $-1.7< \Delta r < -0.7$ cm. The disappearance of the $T_e$ flat might come from that the $q=4$ resonant layer is closer to the LCFS so that the RMP-induced islands touch the limiter, or a stochastic region forms. Around the $q=4$ surface, the density drops with RMPs at $q_a=4.1$ and is consistent with the case with $q_a=4.3$. With RMPs, the sign of the $E_r$ around $q=4$ surface changes from negative to positive at $q_a=4.1$. This is similar to those observed in the cases with $q_a=3.2$ and 4.3. Furthermore, the $E_r$ becomes flattened near the LCFS with RMPs at $q_a=4.1$, i.e., increases inside the LCFS and decreases outside the LCFS.

3.4 Characteristics of turbulence around resonant surfaces with RMPs

The characteristics of turbulence around the resonant surfaces with RMPs are examined for $q_a=4.3$. The root mean square amplitude of the floating potential fluctuations in the frequency band of 30-400 kHz is provided in figure 7 (a). The turbulence intensity drops significantly, by up to 30%, inside the magnetic island, and

![Figure 7](image1.png)

![Figure 8](image2.png)
increases at its boundary. The island effects on turbulence lead to the formation of the negative gradient layer of turbulence intensity in the interval $-1.7 < \Delta r < -1.2$ cm. The radial profiles of the weighted average of the poloidal wave number $k_\theta$ for the turbulence are also shown in figure 7 (b). The $k_\theta$ is calculated with the cross-phase analysis. The negative $k_\theta$ inside the LCFS indicates that the turbulence propagates in the electron diamagnetic drift direction. In the island regime, the $k_\theta$ increases.

The root mean square amplitudes of the floating potential fluctuations in the frequency band of 30-400 kHz with and without RMPs at $q_a=4.1$ are given in figure 8 (a). With RMPs, the turbulence intensity also drops near the q=4 resonant surface of $\Delta r \sim -0.7$ cm. The negative gradient layer of turbulence intensity is established in the interval $-1.7 < \Delta r < -0.5$ cm. The poloidal wave number $k_\theta$ of the turbulence increases in the regime from $\Delta r = -1.5$ to -0.0 cm, as shown in figure 8 (b). In the interval $-0.7 < \Delta r < -0.0$ cm, the sign of the $k_\theta$ changes from negative to positive. The positive $k_\theta$ suggests that the turbulence moves in the ion diamagnetic drift direction.

![Figure 9](image-url)  
Figure. 9 (color online) Radial profiles of the $S(k_\theta)$ spectra for $q_a=4.3$ (a) and $q_a=4.1$ (b) with and without RMPs. ($N_e \sim 2.2 \times 10^{19}$ m$^{-3}$, $B_t \sim 1.9-2.0$ T, $I_p \sim 150$ kA).

The poloidal wave-amplitude spectrum $S(k_\theta)$ of the turbulence is examined for the cases with and without RMPs to obtain more information for the turbulence. The $S(k_\theta)$ spectrum is estimated with two point correlation techniques [37]. Based on the wave number-frequency spectrum $S(k,f) = 1/M \sum_{i=1}^{M} I[k - k_i(f)]S_{crs}(f)$, the
spectral averaged wave number can be derived. Here, \( I(a - b) = 1 \) if \( a = b \), otherwise, \( I(a - b) = 0 \), \( S_{cr,i}(f) \) and \( M \) represent the cross-correlation function and the number of realizations, respectively. Figure 9 (a) presents the \( S(k_0) \) spectra near resonant surfaces with and without RMPs at \( q_a=4.3 \). With RMPs, the \( S(k_0) \) spectra are broadening and the power fraction of turbulence for the positive \( k_0 \) components increases. At \( q_a=4.1 \), the \( S(k_0) \) spectra become wider and the power fraction of turbulence for the positive \( k_0 \) components more significantly increases with RMPs than those of the cases with \( q_a=4.3 \), as shown in figure 9(b). This result suggests that the characteristics of turbulence are significantly changed around resonant surface due to RMPs.

3.5 Turbulent Reynolds stress around resonant surface with RMPs

![Figure 10](image1.png)  
![Figure 11](image2.png)

Figure 10 (color online) Radial profiles of turbulent Reynolds stress (a) and its gradient (b) with and without RMPs at \( q_a=4.3 \).

Figure 11 (color online) Radial profiles of turbulent Reynolds stress (a) and its gradient (b) with and without RMPs at \( q_a=4.1 \).

To understand the interaction of toroidal flows with turbulence around resonant surface, turbulent Reynolds stress and its gradient are measured and presented in
figures 10 (a) and (b) with and without RMPs at \( q_a = 4.3 \). The Reynolds stresses are estimated as \( \langle \delta v_r \delta v_\phi \rangle \), here, \( \delta v_r \) and \( \delta v_\phi \) are the radial and toroidal turbulent velocities, computed from the high frequency components of the turbulence. \( \langle \ldots \rangle \) is the time average over a time period of \( \sim 2 \) ms. The \( \delta v_r \) is estimated with floating potential fluctuations from tips at two poloidal positions. \( \delta v_\phi \) is calculated as \( C_s \delta M_{mach} \). Two steep gradient regimes of Reynolds stresses appear with RMPs. One is localized at the LCFS and another occurs near the \( q=4 \) resonant surface. The steep gradient of Reynolds stresses in the magnetic island region suggests that flows are driven there.

Figures 11 (a) and (b) provide the turbulent Reynolds stress and its gradient with and without RMPs at \( q_a = 4.1 \). With RMPs, the Reynolds stress drops significantly near the \( q=4 \) surface. This differs from the cases with RMPs at \( q_a = 4.3 \), where the Reynolds stress increases. The RMP effects on Reynolds stress induce the increase of the gradient of the turbulent Reynolds stress near the \( q=4 \) surface. This observation is consistent with the measurements of the toroidal flows with and without RMPs at \( q_a = 4.1 \), i.e., the toroidal velocity significantly increases around the \( q=4 \) surface in the direction of the plasma current with RMPs.

### 3.6 Energy transfer between turbulence and toroidal flows

The energy transfer between turbulence and toroidal flows was evaluated. From the turbulent Reynolds stress and the derivative of the toroidal velocity, the flow

![Figure 12](color online) Radial profiles of toroidal flow energy production with and without RMPs at (a) \( q_a = 4.3 \), and (b) \( q_a = 4.1 \).
energy production can be written as \( P = -\langle \partial_r v_x, \partial_r v_x \rangle \frac{dV_x}{dr} \) [38]. Figure 12 (a) gives the radial profiles of the energy production term \( P \) with and without RMPs at \( q_a=4.3 \). The positive (negative) \( p \) indicates the energy source (sink) for the toroidal flows. Without RMPs, the peaked energy production appears near the LCFS. With RMPs, two positive peaks for the flow energy production occur. One is localized near the LCFS, and another is near the \( q=4 \) resonant surfaces. Figure 12(b) provides the radial profiles of the energy production term \( P \) with and without RMPs at \( q_a=4.1 \). At \( q_a=4.1 \), without RMPs, the shape of the radial profiles for the flow energy production is similar to the case at \( q_a=4.3 \), i.e., the peak of the flow energy production occurs near the LCFS. However, with RMPs, the peak of the flow energy production moves to near the \( q=4 \) resonant surface. The result suggests that turbulence energy transfers into toroidal flows near the \( q=4 \) resonant surface with RMPs. In addition, the energy sink is significantly observed at \( q_a=4.3 \) with RMPs.

### 3.7 Conclusion and discussion

The toroidal rotation flows around the resonant surfaces with resonant magnetic perturbations are studied. These experiments were performed using a Langmuir probe array in the edge plasmas of the J-TEXT tokamak. Some common features were obtained. With RMPs, the toroidal rotation around resonant surfaces increases in the direction of the plasma current. The characteristics of the turbulence around resonant surface are significantly affected by RMPs. The turbulence intensity changes and the \( k_\theta \) increases with RMPs. The power fraction of the turbulence components in the ion diamagnetic drift direction increases with RMPs. The measurements of turbulence Reynolds stresses are consistent with that the toroidal flows may be driven by turbulence. The estimations of the energy transfer suggest that turbulence energy transfers into toroidal flows.

The observation shows that the acceleration of the co-current toroidal rotation with RMPs is well correlated with the change of turbulence characteristics. The measurements of the turbulent stresses and the energy transfer between flows and turbulence with and without RMPs suggests that the momentum (energy)
redistribution takes place due to the turbulence force with RMPs, i.e., the momentum (energy) sources or sinks occur near the resonant surface. Thus, the observation has the implication of the intrinsic rotation being affected by RMPs. This result suggests that RMPs can be as a tool to change the characteristics of the edge turbulence, and thus control the intrinsic rotations in the edge tokamak plasmas.

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